

# Good Day!

- There are answer keys to the homework on either side of the room.
- Look at the answers and write the number of the problem that you would most like to see solved on your whiteboard.

# Most Requested Problem

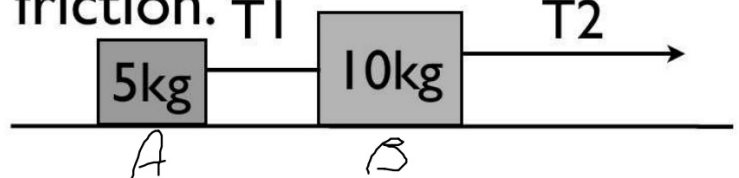
# Today

- Problems with multiple tensions.
- Multi-body problems.
- Atwood Machines

# Tension

- If a tension is causing the acceleration of an object, we can apply  $F=ma$  to find the tension.
- Until now: we have assumed the total tension in a chord/string to be uniform.
- We can use  $F=ma$  to find out the individual tensions on each side of a chord/cable.

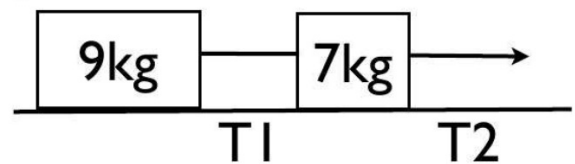
The blocks are accelerating at  $2.5 \text{ m/s}^2$ .  
Find the tensions on each string. Assume  
no friction.  $T_1$



$$T_1 = m_A \cdot a = 5 \text{ kg} \cdot 2.5 \text{ m/s}^2 = 12.5 \text{ N}$$

$$T_2 = (m_A + m_B) \cdot 2.5 \text{ m/s}^2 = 37.5 \text{ N}$$

The tension on  $T_1$  is  $45\text{N}$ . Find the acceleration of the system and  $T_2$ .



# Atwood's Machine

- Two masses hung over a pulley.
- We assume that the pulley is massless and frictionless. The rope is massless.
- Calculate the acceleration in the system and the tension on the rope.
- We need to pick a positive direction.

$m_1 = 7\text{kg}$ .  $m_2 = 5\text{kg}$ . Acceleration of the system and the tension on each rope. How can we rearrange the system to a simpler picture?

④

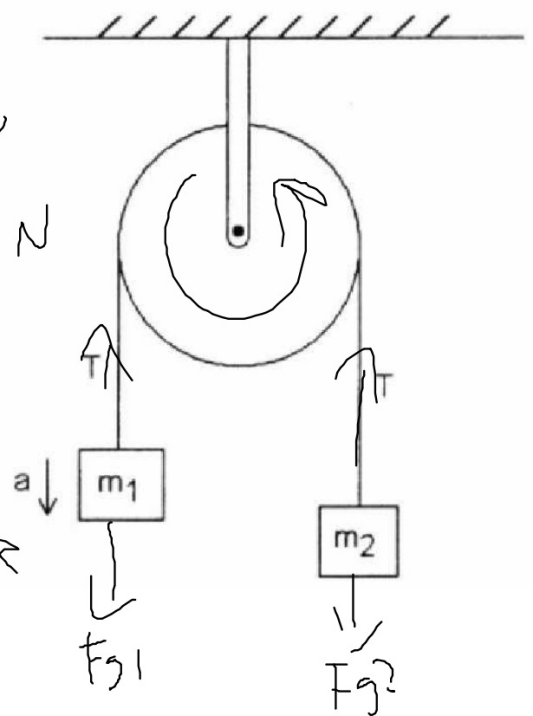


$$\Sigma F = 68.6\text{ N} - 49\text{ N} = 19.6\text{ N}$$

$$\Sigma m = 12\text{ kg}$$

$$\Sigma F = \Sigma m \cdot a$$

$$a = F/m = 1.63\text{ m/s}^2$$



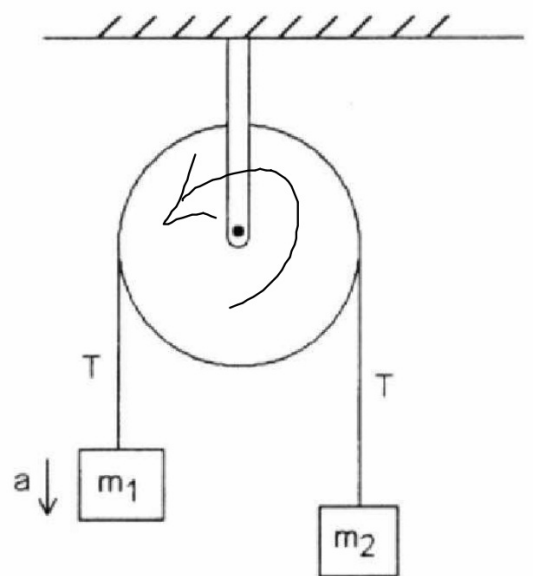


$m_1 = 7\text{kg}$ .  $m_2 = 5\text{kg}$ . Acceleration of the system and the tension on each rope. How can we rearrange the system to a simpler picture?

$$\Sigma F = 68.6\text{N} - 49\text{N}$$

$$\Sigma m = 12\text{kg}$$

$$a = \frac{F}{m} = 1.63\text{m/s}^2$$



Randall Munroe:

# Comics that ask "what if?"

TED2014 · 9:29 · Filmed Mar 2014  
Subtitles available in 21 languages

 [View interactive transcript](#)



## Serious Force



MIT Physics Demo -- Low Friction Atwood Machine

# Video Atwood

Do Now: Solve for the acceleration of the system.

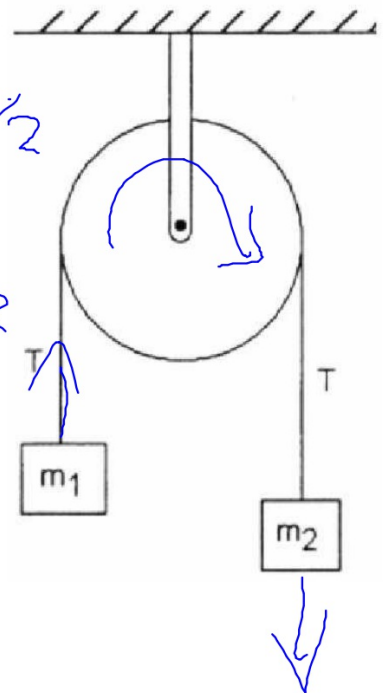
$m_1 = 0.55\text{kg}$ .  $m_2 = 0.56\text{kg}$ . Find the acceleration of the system.

knowns:

$$F_{g1} = m_1 g = 0.55\text{kg} \cdot 9.8\frac{\text{m}}{\text{s}^2} \\ \textcircled{5.39\text{N}}$$

$$F_{g2} = m_2 g = 0.56\text{kg} \cdot 9.8\frac{\text{m}}{\text{s}^2} \\ \textcircled{5.49\text{N}}$$

$$a = 0.088\frac{\text{m}}{\text{s}^2}$$



Does this agree with the kinematics answer?  $V_i=0\text{m/s}$ .  $\Delta x=1\text{m}$ .  $t=4.79\text{s}$ .  $a=?$

$$\Delta x = V_i t + \frac{1}{2} a t^2$$

$$\frac{2\Delta x}{t^2} = \frac{a t^2}{t^2}$$

$$\Rightarrow a = \frac{2\Delta x}{t^2}$$

$$0.087 \text{ m/s}^2$$



# Multiple Tension on One Rope

- We know that the total tension on a rope is equal to the mass of the **system** times the acceleration of the system.
- The tension on either side of a rope can actually be different.
- That tension is the tension needed to accelerate each object at the same rate.

$m_1 = 5\text{kg}$ .  $m_2 = 3\text{kg}$ . Find the tension of the rope **at** each block. Find the total tension in the chord.

